## HARFORD COUNTY PUBLIC SCHOOLS

MATHEMATICS 6 CURRICULUM

## CLICK HERE for the Maryland College and Career Ready Standards for Grade 6 Mathematics.

## Topic 1: Use Positive Rational Numbers

Primary Resource: enVisionmath2.0 Grade 6, Pearson Savvas, 2017.

## Enduring Understandings

- Topic 1 focuses on the deep understanding of our number system through fluency in computations with decimals and fractions. Students use all four operations with decimals before multiplying and dividing with fractions and mixed numbers. Students apply these skills to solve real-world problems.


## Essential Questions

- How can you fluently add, subtract, multiply and divide decimals?
- How can you multiply and divide fractions?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Fluently Add, Subtract, and <br> Multiply Decimals | Algorithms can be used to add, subtract, and multiply decimals fluently. | 6.NS.B.3 |
| Fluently Divide Whole Numbers <br> and Decimals | An algorithm can be used to divide whole numbers and decimals fluently. | 6.NS.B.2 <br> $6 . N S . B .3$ |
| Multiply Fractions | Visual models such as area models and number lines can be used to multiply fractions. The <br> product of two fractions can be found by multiplying the numerators and then the <br> denominators. Multiplying mixed numbers is an extension of multiplying fractions. | 6.NS.A.1 |
| Stocking up | Many real-world problem situations can be represented with a mathematical model, but that <br> model may not represent a real-world situation exactly. | 6.NS.B.3 |

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| Understand Division with Fractions | Visual models, such as area models and number lines, and equations can be used to represent <br> and solve problems that involve division of fractions. Dividing a whole number by a fraction <br> is equivalent to multiplying the whole number by the reciprocal of the fraction. | 6.NS.A. 1 |
| :--- | :--- | :--- |
| Divide Fractions by Fractions | Visual models, such as area models and number lines, can be used to represent and solve <br> problems that involve division of a fraction by a fraction. Dividing by a fraction is <br> equivalent to multiplying by the fraction's reciprocal. | 6.NS.A.1 |
| Divide Mixed Numbers | The quotient of mixed numbers can be found by writing the mixed numbers as fractions and <br> multiplying the dividend by the divisor's reciprocal. Students estimate and multiply to check <br> their answers. | 6.NS.A.1 |
| Solve Problems with Rational <br> Numbers | Multi-step problems require students to carefully plan the steps they follow to find the <br> solution. Fraction and decimal problems require precision for students to identify the steps <br> needed to solve the problem, use correct information, and calculate accurately. | 6.NS.A.1 |

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## Topic 2: Integers and Rational Numbers

## Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 2 focuses on applying and extending previous understandings of numbers to the system of rational numbers, including developing a deep understanding of integers and other rational numbers, and locating points associated with rational number ordered pairs on the coordinate plane.


## Essential Questions

- What are integers and rational numbers?
- How are points graphed on a coordinate plane?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Understand Integers | Integers are the counting numbers, their opposites, and zero. Integers can be <br> compared, ordered, and used to describe real-world contexts. | 6.NS.C.5 <br> 6.NS.C.6a <br> 6.NS.C.6c |
| Represent Rational Numbers on the <br> Number Line | Each rational number can be associated with a unique point on the number line. <br> A number to the right of another on the number line is the greater number. | 6.NS.C.7a <br> 6.NS.C.7b |
| Absolute Values of Rational Numbers | The absolute value of a number can be described as the number's distance from zero <br> on the number line. Absolute value can be interpreted as the magnitude of a positive <br> or negative quantity in a real-world situation. | 6.NS.C.7c <br> 6.NS.C.7d |
| Represent Rational Numbers on the <br> Coordinate Plane | The absolute value of a number can be described as the number's distance from zero <br> on the number line. Absolute value can be interpreted as the magnitude of a positive <br> or negative quantity in a real-world situation. | 6.NS.C.6b <br> 6.NS.C.6c |
| Find Distances on the Coordinate Plane | Many real-world problem situations can be represented with a mathematical model, <br> but that model may not represent a real-world situation exactly. | 6.NS.C.5 <br> 6.NS.C.7d |


| Find Distances on the Coordinate Plane | The distance between two points on the coordinate plane with the same first <br> coordinate or the same second coordinate can be found by adding or subtracting the <br> absolute values of the coordinates that differ. | 6.NS.C.8 |
| :--- | :--- | :--- |
| Represent Polygons on the Coordinate <br> Plane | The coordinates of the vertices of a polygon on the coordinate plane can be used to <br> find the lengths of the sides of the polygon and its perimeter. | 6.G.A.3 <br> 6.NS.C.8 |

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## Topic 3: Numeric and Algebraic Expressions

## Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 3 applies and extends previous understandings of arithmetic and numerical expressions to greatest common factors, least common multiples, and algebraic expressions. Students interpret, evaluate, and write algebraic expressions, including expressions with exponents, in both mathematical and real-world contexts.


## Essential Questions

- What are integers and rational numbers?

| Lesson Title | Lesson Overview | Standards |  |
| :--- | :--- | :--- | :--- |
| Understand and Represent Exponents | A whole number exponent can be used to represent repeated multiplication of a <br> number. | Any number can be written as its prime factorization. The greatest common factor <br> (GCF) is the greatest factor that two or more whole numbers have in common. The <br> least common multiple (LCM) is the smallest multiple that two or more non-zero <br> whole numbers have in common. | 6.NS.B.4 |
| Find Greatest Common Factor and Least <br> Common Multiple | There is an agreed-upon order in which operations are carried out in a numerical <br> expression. | 6.EE.A.1 <br> 6.EE.A.3 |  |
| Write and Evaluate Numerical <br> Expressions | Algebraic expressions use variables to describe situations in which some of the <br> information is not known. Parts of expressions can be described using words such as <br> term, coefficient, product, and factor. | 6.EE.A.2a <br> 6.EE.A.2b <br> 6.EE.B.6 |  |
| Write Algebraic Expressions | The value of an algebraic expression can be found by replacing the variables with <br> given numbers and doing the calculation that results. | 6.EE.A.2c <br> 6.EE.B.6 |  |
| Evaluate Algebraic Expressions | Many real-world problem situations can be represented with a mathematical model, <br> but that model may not represent a real-world situation exactly. |  |  |
| Modeling the Field Trip |  |  |  |


| Generate Equivalent Expressions | The Distributive Property and other properties of operations are used to identify and <br> write equivalent expressions. | 6.EE.A.3 <br> 6.EE.A.4 |
| :--- | :--- | :--- |
| Simplify Algebraic Expressions | The Distributive Property and other properties of operations are used to identify and <br> write equivalent expressions. | 6.EE.A.3 <br> 6.EE.A. 4 |

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## Topic 4: Represent and Solve Equations and Inequalities

## Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 4 focuses on solving one-step equations and simple inequalities as well as analyzing the relationship between two quantities when one quantity, the dependent variable, changes in relationship to the other quantity, the independent variable. Students develop a deep understanding of algebraic equations and solve them by applying properties of equality and inverse operations. Solutions to inequalities are graphed on a number line. Students represent the relationships between the dependent and independent variables in tables, graphs, and equations.


## Essential Questions

- What procedures can be used to write and solve equations and inequalities?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Understand Equations and Solutions | A solution of an equation is a value for the variable that makes the equation true. An <br> equation is true when the expressions or numbers on both sides of the equal sign <br> have the same value. | 6.EE.B.5 |

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| Understand and Write Inequalities | An inequality is a mathematical sentence that contains the inequality symbol $<$ (is <br> less than), $>$ (is greater than), $\leq$ (is less than or equal to), $\geq$ (is greater than or equal <br> to), or $\neq$ (is not equal to). An inequality describes a situation that has an infinite <br> number of numerical possibilities. | 6.EE.B. 8 <br> $6 . E E . B .5$ |
| :--- | :--- | :--- | :--- |
| Solve Inequalities | An inequality is a mathematical sentence that contains the inequality symbol $<$ (is <br> less than), $>$ (is greater than), $\leq$ (is less than or equal to), $\geq$ (is greater than or equal <br> to), or $\neq$ (is not equal to). An inequality describes a situation that has an infinite <br> number of numerical possibilities. | 6.EE.B. 8 <br> $6 . E E . B .5$ |
| Checking a Bag | Many real-world problem situations can be represented with a mathematical model, <br> but that model may not represent a real-world situation exactly. | 6.EE.B. 8 <br> $6 . E E . B .5$ <br> $6 . E E . B .6$ |
| Understand Dependent and Independent <br> Variables | Variables can be used to represent quantities that change in relationship to one <br> another. The dependent variable changes in response to the independent variable. | 6.EE.C.9 |
| Use Patterns to Write and Solve | Patterns can be used to identify the relationship between quantities and write an <br> equation that describes the relationship. | 6.EE.C.9 |
| Relate Tables, Graphs, and Equations | Tables, graphs, and equations can be used to analyze the relationship between <br> dependent and independent variables. | 6.EE.C.9 |

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## Topic 5: Understand and Use Ratio and Rate

## Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 5 focuses on developing an understanding of ratios and rates and the ways that they can be used to solve problems.


## Essential Questions

- What are ratios and rates?
- How can you use ratios and rates to describe quantities and solve problems?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Understanding Ratios | Ratios can be used to describe the relationship between two quantities where for every <br> $x$ unit of one quantity, there are $y$ units of another quantity. | 6.RP.A.1 |
| Generate Equivalent Ratios | Equivalent ratios can be found by multiplying or dividing both terms by the same <br> nonzero number. | 6.RP.A.3a |
| Comparing Ratios | Ratio tables can be used to compare ratios and solve problems. | 6.RP.A.3a |
| Represent and Graph Ratios | Equivalent ratios can be represented in a table, and the pairs of values can be plotted <br> on a coordinate plane. | 6.RP.A.3a |
| Understand Rates and Unit Rates | A rate is a special type of ratio that compares two quantities with different units of <br> measure. A unit rate is a special rate that compares a quantity to one unit of another <br> quantity. | 6.RP.A.2 <br> 6.RP.A.3a <br> 6.RP.A.3b |
| Compare Unit Rates | Rates are easily compared when they are expressed as unit rates. | 6.RP.A.3a <br> 6.RP.A.3b |
| Solve Unit Rate problems | Unit rates, including unit prices, can be used to solve problems. | 6.RP.A.3b |

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| Get in Line | Many real-world problem situations can be represented with a mathematical model, <br> but that model may not represent a real-world situation exactly. | 6.RP.A.2 <br> 6.RP.A.3b |
| :--- | :--- | :--- |
| Ratio Reasoning: Convert Customary Unit | Unit rates and conversion factors can be used to convert customary units of measure. | 6.RP.A.3d |
| Ratio Reasoning: Convert Metric Units | Unit rates and conversion factors can be used to convert metric units of measure. | 6.RP.A.3d |
| Relate Customary and Metric Units | Unit rates and conversion factors can be used to convert between customary and <br> metric units of measure. | 6.RP.A.3d |

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## Topic 6: Understand and Use Percent

Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 6 focuses on understanding percent and using percent to solve problems. Students use models to represent percents. They use reasoning, equivalent rates, and division to find the relationship among fractions, decimals, and percents. Students use this relationship to find percents greater than 100 and less than one.


## Essential Questions

- What is the meaning of percent?
- How can percent be estimated and found?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Understand Percent | A percent is a rate in which the first term is compared to 100. The percent is the <br> number of hundredths that represent the part of the whole. | 6.RP.A.3c |
| Relate Fractions, Decimals, and Percents | Fractions, decimals, and percents are three ways to show parts of a whole. | 6.RP.A.3c |
| Represent Percents Greater Than 100 or <br> Less Than 1 | A percent greater than 100 is equivalent to more than the whole. A percent less than <br> 1 is equivalent to less than $1 / 100$ of the whole. | 6.RP.A.3c |
| Estimate to Find a Percent | Equivalent fractions and compatible numbers can be used to estimate the percent of <br> a number. | 6.RP.A.3c |
| Find the Percent of a Number | Finding the percent of a whole is like finding the fractional part of a whole. | 6.RP.A.3c |
| Find the whole given a part and the <br> percent | Models and equations can be used to find the whole amount when the percent and a <br> part are known. | 6.RP.A.3c |
| Ace the Test | Many real-world problem situations can be represented with a mathematical model, <br> but that model may not represent a real-world situation exactly. | 6.RP.A.3c <br> 6.RP.A.1 |

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## Topic 7: Solve Area, Surface Area, and Volume Problems

Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 7 focuses on a deep understanding of areas of polygons, surface areas of solids, and volumes of right rectangular prisms with fractional side lengths.


## Essential Questions

- How can the areas of certain shapes be found?
- What are the meanings of surface area and volume?
- How can surface area and volume be found?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Find Areas of Parallelograms and <br> Rhombuses | The formula for the area of a parallelogram, $A=b h$, can be derived from the <br> formula for the area of a rectangle. | 6.G.A.1 <br> 6.EE.A.2c |
| Solve Triangle Area Problems | The formula for the area of a triangle, $A=\frac{1}{2} b h$, can be derived from the formula <br> for the area of a parallelogram. | 6.G.A.1 <br> 6.EE.A.2c |
| Find Areas of Trapezoids and Kites | The areas of trapezoids and kites can be found by decomposing the trapezoids and <br> kites into shapes for which the area formulas are known. | 6.G.A.1 <br> 6.EE.A.2c |
| Find Areas of Polygons | The areas of polygons, including polygons on the coordinate plane, can be found by <br> composing or decomposing the polygons into shapes for which the area formulas <br> are known. | 6.G.A.1 <br> 6.EE.A.2c |
| Represent Solid Figures Using Nets | A solid figure can be classified based on the number of bases, the shape of the <br> base(s), and the shape of the other faces. A net can be used to represent a <br> polyhedron. | 6.G.A.4 |
| That's a Wrap | Many real-world problem situations can be represented with a mathematical model, <br> but that model may not represent a real-world situation exactly. | 6.G.A.4 <br> 6.EE.A.2c |

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|  |  |  |
| :--- | :--- | :--- |
| Find Surface Areas of Prisms | The surface area of a prism is the sum of the areas of its faces. | 6.G.A.4 |
| 6.EE.A.2a |  |  |
| 6.EE.A.2c |  |  |
| Find Surface Areas of Pyramids | The surface area of a pyramid is the sum of the areas of its faces. |  |
|  |  | 6.G.A.4 |
| Find Volumes with Fractional Edge <br> Lengths | Unit cubes or formulas can be used to find the volume of rectangular prisms and <br> cubes. | 6.EE.A.2a <br> 6.EE.A.2c |
| 6.EE.B.6 |  |  |

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## Topic 8: Display, Describe, and Summarize Data

## Primary Resource: enVisionmath2.0 Grade 6, Pearson, 2017.

## Enduring Understandings

- Topic 8 focuses on developing an understanding of variability and the concept of statistical measures. Students learn to recognize statistical questions, describe, and summarize data using measures of center and variability, and display data using boxplots and histograms.


## Essential Questions

- How can data be described by a single number?
- How can tables and graphs be used to represent data and answer questions?

| Lesson Title | Lesson Overview | Standards |
| :--- | :--- | :--- | :--- |
| Recognize Statistical Questions | A statistical question anticipates variability in responses and can be answered by <br> collecting and analyzing data. | 6.SP.A.1 <br> 6.SP.B.4 |
| Summarize Data using Mean, Median, <br> Mode and Range | The mean, median, and mode are measures that can be used to describe the center <br> of a data set. The range is a measure that can be used to describe the variability of <br> a data set. | 6.SP.A.3 <br> 6.SP.B.5c |
| Display Data in Box Plots | A box plot is a good choice for displaying a distribution of numerical data values <br> on a number line. | 6.SP.A.4 |
| Display Data in Frequency Tables and <br> Histograms | Data values can be organized into equal intervals and displayed in a frequency <br> table or histogram. | 6.SP.A.4 <br> 6.SP.B.5a |
| Summarize Data Using Measures of <br> Variability | Measures of variability, such as the mean absolute deviation (MAD) and <br> interquartile range (IQR), describe the spread and clustering of data in a set. | 6.SP.B.5c <br> 6.SP.B.4 |
| Choose Appropriate Statistical Measures | Data sets may best be described using different measures of center and variability. | 6.SP.B.5d <br> 6.SP.B.5c |

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|  |  |  | 6.SP.A.2 |
| :--- | :--- | :--- | :--- |
| Summarize Data Distributions | A set of numerical data collected to answer a statistical question has a distribution <br> that can be described by its center, spread, and overall shape. | 6.SP.B. 4 <br> 6.SP.B. 5 b |  |
|  |  | 6.SP.B.5c |  |
|  |  | 6.SP.A.2 |  |
|  | Many real-world problem situations can be represented with a mathematical | 6.SP.A.3 |  |
|  | model, but that model may not represent a real-world situation exactly. | 6.SP.B.5a |  |
|  |  | 6.SP.B.5b |  |
|  |  | 6.SP.B.5c |  |

